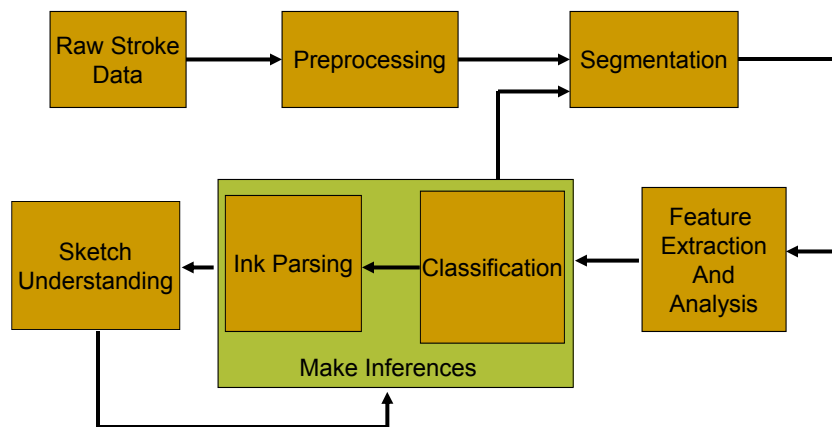


Ink Parsing in Sketch-Based Interfaces

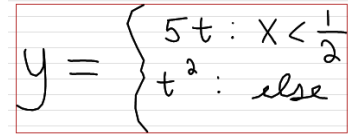
Lecture #10: Ink Parsing
 Joseph J. LaViola Jr.
 Fall 2013

Recall Pen-Based Interface Dataflow

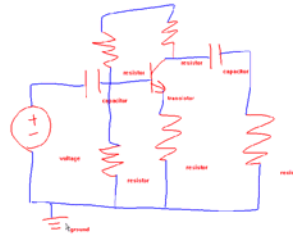


Sketch Parsing

- Often recognition of strokes is insufficient
 - except for gestures
- Require an understanding of spatial relationships
 - good examples are mathematical expressions
- Higher level classifications
 - is it a word or a drawing?



$$y = \begin{cases} 5t & : X < \frac{1}{2} \\ t^2 & : \text{else} \end{cases}$$



www.engr.ucr.edu/~stahov/research/acsparc.htm

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CAP 6105 – Pen-Based User Interfaces

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Approaches to Sketch Parsing

- Top down vs. bottom up
- Focus on mathematical expressions
 - 2D (coordinate) grammars
 - graph rewriting
 - useful for other types of parsing as well (diagrams, tables, lists, etc...)
 - projection profile cutting
 - procedurally coded syntax rules
 - stochastic grammars
- Other parsing approaches
 - conditional random fields
 - statistical visual languages
 - many others

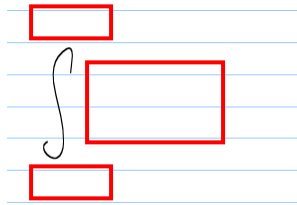
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2D Grammars

- Grammar + spatial relationship rules
 - useful if a well defined syntax exists
 - looks for key symbols
- One Approach – Box Grammar
 - divide input into distinct areas based on symbol found



Graph Rewriting

- Expressions represented as nodes and arcs
- Rewrite rules applied to graph to reduce it progressively
 - rules are also subgraphs
 - graph reduced to single node representing expression

Graph Rewriting Example (Blostein and Grbavec 1996)

- Build
 - add edges between symbols (above, below, left, superscript, subscript)
- Constrain
 - Apply knowledge of notational conventions
 - remove contradictory associations
 - disambiguate horizontal lines
 - disambiguate dots
 - disambiguate diagonal associations
- Rank
 - Use information about operator precedence to group symbols into subexpressions
- Incorporate
 - Interpret subexpressions

Projection Profile Cutting

- Used primarily in document analysis
- Uses horizontal and vertical projections of expression onto x and y axis
 - subdivides expression recursively
- Problem with expressions where symbols are close together (no white space)

Procedurally Coded Syntax Rules

- Observations about domain coded programmatically
 - similar to rule based approach for recognition
- Sample rule for horizontal line

A length threshold of 20 pixels is used to classify a horizontal line as a short or long bar.

If it is a long bar and has symbols above and below, it is treated as a division.

If there are no symbols above, it is treated as a boolean negation.

If a short bar has no symbols above or below, it is treated as minus sign.

If it has symbols above or below, the combination symbols such as =, \leq , and \geq are formed.

Stochastic Grammars

- Used to deal with noisy data and spatial ambiguities
- Probabilities associated with each production rule
- For any sequence in a given parse – probability can be calculated
- Requires training

MathPad² Parsing Approach

- Uses 2D coordinate grammar approach with some syntax rules
- Basic approach
 - preprocessing step (for functions)
 - sort list of symbols
 - parse functions – use grammar
 - process functions – handle spatial relationship testing
 - intermixed with parse functions

Grammar (1)

```

<math_formula> ::= <equation> | <expression>
<equation> ::= <expression> <relational_op> <expression> |
<expression> '=' <cond_expression>
<relational_op> ::= '=' | '<=' | '<' | '>' | '<=' | '>='
<cond_expression> ::= '{' <cond_statement>
<cond_statement> ::= 'if' <expression> ':' <logic_expression>
{'elseif' <expression> ':' <logic_expression> }
<expression> ':' else'
<logic_expression> ::= <equation> <logical_op> <logic_expression> | <equation>
<logical_op> ::= 'and' | 'or'
<expression> ::= <term> '+' <expression> |
<term> '-' <expression> |
<term> '^' <expression> |
<term>
<term> ::= <factor> '*' <term> |
'(' <expression> ')' |
<factor>
<factor> ::= <sub_expression> '/' <factor> |
<sub_expression>
<sub_expression> ::= <integral> | <derivative> | <summation> |
<function> | <terminal>

```

Grammar (2)

```

<integral>      ::= 'int(' <expression> ',,' <variable> '(') |
                  'int(' <expression> ',,' <variable> ',,'
                    <expression> ',,' <expression> ')')
<derivative>   ::= 'diff(' <expression> ',,' <variable> '(') |
                  'diff(' <expression> ',,' <variable> ',,'
                    <integer> '(')
<summation>    ::= 'sum(' <expression> '(') |
                  'sum(' <expression> ',,' <expression> ',,'
                    <expression> '(')
<function>     ::= <func_name> '(' <expression> '(')
<func_name>    ::= 'sqrt' | 'abs' | 'log' | 'exp' |
                  'sin' | 'cos' | 'tan' | 'asin' |
                  'acos' | 'atan'
<terminal>    ::= <variable> | <number>
<variable>    ::= <letter> |
                  <letter> '_' {<integer>} {<letter>} {<integer>}
<number>      ::= <integer> |
                  <integer> '.' <unsigned_int>
<integer>     ::= <sign> <unsigned_int> | <unsigned_int>
<unsigned_int> ::= <digit> <unsigned_int> | <digit>
<sign>       ::= '+' | '-'
<digit>      ::= [0-9]
<letter>     ::= [a-z] | [A-Z] | [alpha-zeta]

```

Parse functions

- High level parse
- Expression parse
- Sub-expression parse
- Symbol specific parsing
 - square root parse
 - integration parse
 - summation parse
 - fraction parse
- Factor parse
- Term parse

$$\frac{2 \int x^2 dx}{(x-4y)^8}$$

$$\frac{6x + y}{3 + \sin(x)}$$

Process functions

- Provide parse functions important info
- Deal with spatial relationships
 - implicit operators
 - fractions and square roots
 - summations , derivatives, integrals
 - Conditionals

$$x(t+h) = \begin{cases} l-r : x(t) > (l-r) \\ r : x(t) < r \\ x(t) + vh : \text{else} \end{cases}$$

Reducing parsing decisions

- Use application to reduce decisions
- Implicit operators (no numbers have subscripts)
- Correct trig functions 5in -> sin
- Functions of time f(+) -> f(t)

Readings

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- Ye, Ming, and Paul Viola. Learning to Parse Hierarchical Lists and Outlines Using Conditional Random Fields. *International Workshop on Frontiers in Handwriting Recognition*, 2004.
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