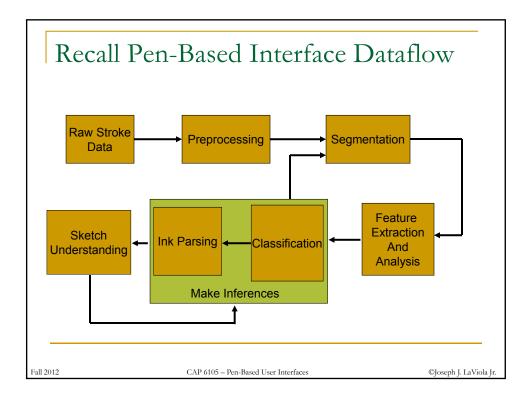
# Ink Parsing in Sketch-Based Interfaces

Lecture #10: Ink Parsing Joseph J. LaViola Jr. Fall 2012

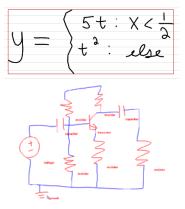
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## Sketch Parsing

- Often recognition of strokes is insufficient
  - except for gestures
- Require an understanding of spatial relationships
  - good examples are mathematical expressions
- Higher level classifications
  - is it a word or a drawing?



www.engr.ucr.edu/~stahov/research/acsparc.htm

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## Approaches to Sketch Parsing

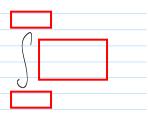
- Top down vs. bottom up
- Focus on mathematical expressions
  - 2D (coordinate) grammars
  - graph rewriting
    - useful for other types of parsing as well (diagrams, tables, lists, etc...)
  - projection profile cutting
  - procedurally coded syntax rules
  - stochastic grammars
- Other parsing approaches
  - conditional random fields
  - statistical visual languages
  - many others

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## 2D Grammars

- Grammar + spatial relationship rules
  - useful if a well defined syntax exists
  - looks for key symbols
- One Approach Box Grammar
  - divide input into distinct areas based on symbol found



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## Graph Rewriting

- Expressions represented as nodes and arcs
- Rewrite rules applied to graph to reduce it progressively
  - rules are also subgraphs
  - graph reduced to single node representing expression

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## Graph Rewriting Example (Blostein and Grbavec 1996)

- Build
  - add edges between symbols (above, below, left, superscript, subscript)
- Constrain
  - Apply knowledge of notational conventions
    - remove contradictory associations
    - disambiguate horizontal lines
    - disambiguate dots
    - disambiguate diagonal associations
- Rank
  - Use information about operator precedence to group symbols into subexpressions
- Incorporate
  - Interpret subexpressions

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## Projection Profile Cutting

- Used primarily in document analysis
- Uses horizontal and vertical projections of expression onto x and y axis
  - subdivides expression recursively
- Problem with expressions where symbols are close together (no white space)

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## Procedurally Coded Syntax Rules

- Observations about domain coded programmatically
   similar to rule based approach for recognition
- Sample rule for horizontal line

A length threshold of 20 pixels is used to classify a horizontal line as a short or long bar.

If it is a long bar and has symbols above and below, it is treated as a division.

If there are no symbols above, it is treated as a boolean negation.

If a short bar has no symbols above or below, it is treated as minus sign.

If it has symbols above or below, the combination symbols such as =,  $\leq$ , and  $\geq$  are formed.

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#### Stochastic Grammars

- Used to deal with noisy data and spatial ambiguities
- Probabilities associated with each production rule
- For any sequence in a given parse probability can be calculated
- Requires training

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## MathPad<sup>2</sup> Parsing Approach

- Uses 2D coordinate grammar approach with some syntax rules
- Basic approach
  - preprocessing step (for functions)
  - sort list of symbols
  - □ parse functions use grammar
  - process functions handle spatial relationship testing
    - intermixed with parse functions

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## Grammar (1)

```
<math_formula>
                  ::= <equation> | <expression>
<equation> ::= <expression> <relational_op> <expression> |
                   <expression> ''='' <cond_expression>
<relational_op> ::= '(=') | '('=') | '('>') | '('>=') | '('>=')
<cond_expression> ::= ''{'' <cond_statement>
<cond_statement> ::= ''if'' <expression> '':'' <logic_expression>
                   {''elseif', <expression> '':', <logic_expression> }
                    <expression> '': else''
<logic_expression> ::= <equation> <logical_op> <logic_expression> | <equation>
<logic_op> ::= ''and'' | ''or''
                 ::= <term> ('+') <expression> |
<expression>
                    <term> ''-'' <expression>
                     <term> ''^' <expression> |
                     <term>
                 ::= <factor> ''*', <term>
<term>
                     ''('' <expression> '')'' |
                     <factor>
                 ::= <sub_expression> ''/', <factor> |
                     <sub_expression>
<sub_expression>
                 ::= <integral> | <derivative> | <summation> |
                     <function> | <terminal>
```

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## Grammar (2)

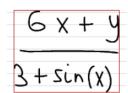
```
<integral>
<derivative>
             ::= ''sum('' <expression> '')''
<summation>
                "('sum(('(expression>'(',')'(expression>'(',')'(expression>'(',')')')")"
             <function>
<func_name>
             ::= <variable> | <number>
<terminal>
             <variable>
             <number>
             ::= <sign> <unsigned_int> | <unsigned_int>
<integer>
             ::= <digit> <unsigned_int> | <digit> ::= ''+'' | ''-''
<unsigned_int>
<sign>
<digit>
             ::= [0-9]
             ::= [a-z] | [A-Z] | [alpha-zeta]
<letter>
```

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#### Parse functions

- High level parse
- Expression parse
- Sub-expression parse
- Symbol specific parsing
  - square root parse
  - integration parse
  - summation parse
  - fraction parse
- Factor parse
- Term parse





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## Process functions

- Provide parse functions important info
- Deal with spatial relationships
  - implicit operators
  - fractions and square roots
  - summations, derivatives, integrals
  - Conditionals

$$X(t+h) = \begin{cases} l-r : X(t) > (l-r) \\ r : X(t) < r \\ X(t) + Vh : else \end{cases}$$

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## Reducing parsing decisions

- Use application to reduce decisions
- Implicit operators (no numbers have subscripts)
- Correct trig functions 5in -> sin
- Functions of time f(+) -> f(t)

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## Readings

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