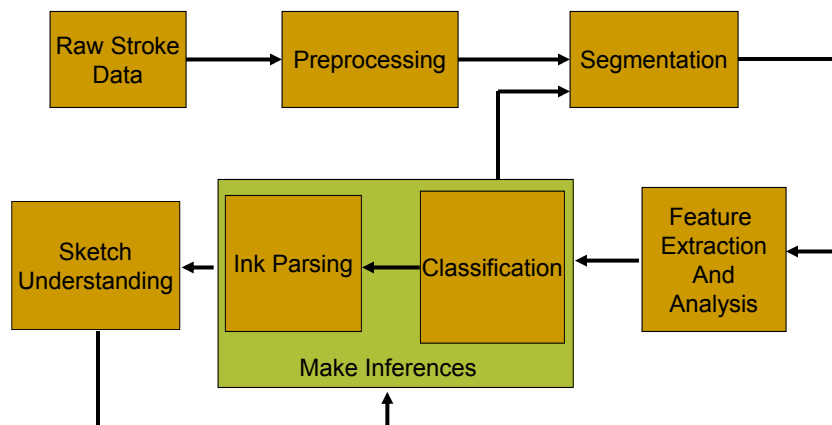


Features Extraction for Sketch-Based Recognition

Lecture #9: Feature Extraction
Joseph J. LaViola Jr.
Fall 2012

Recall Pen-Based Interface Dataflow



Feature Extraction and Analysis

- What came first, the feature or the machine learning algorithm?
- Want to distinguish sketch components from one another
- Good features are critical
- Extract important information
 - geometrical, statistical, contextual
- Examples include
 - arc length, histograms, cusps, aspect ratio
 - self-intersections, stroke area, etc...

Finding Features

- Challenging problem
 - need fast algorithms for gathering information
 - features must be good discriminators
- Often trial and error
- Can be domain specific

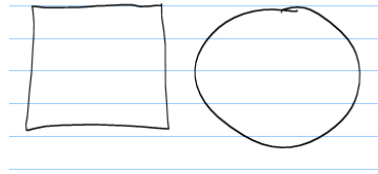
Geometric Features (1)

■ Number of strokes

- if you know how many strokes a symbol has, you can break up your recognizer into pieces (i.e., recognizer for 1 stroke symbols, recognizer for 2 stroke symbols ...)

■ Cusps

- smooth vs. jagged strokes
- distance between cusps
 - useful for when cusps are close together/far apart



Fall 2012

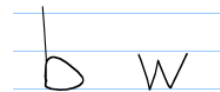
CAP 6105 – Pen-Based User Interfaces

©Joseph J. LaViola Jr.

Geometric Features (2)

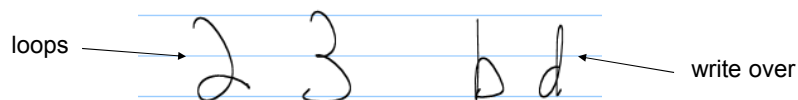
■ Aspect ratio (width / height)

- tall vs. flat



■ Self Intersections

- loops vs. no loops
- strokes with write over
- distance between self intersections also useful
- use line segment intersection algorithm



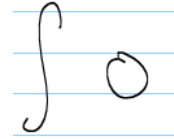
Fall 2012

CAP 6105 – Pen-Based User Interfaces

©Joseph J. LaViola Jr.

Geometric Features (3)

- First and last distance
 - Strokes where first and last points are close together vs. far apart
 - simple computation – $\|p_n - p_1\|$
- Arc length
 - many different symbols have varying arc lengths
 - simple computation as well –



$$l = \sum_{i=2}^n \|p_i - p_{i-1}\|$$

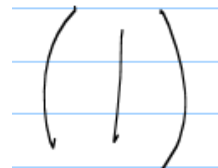
Geometric Features (4)

- Stroke area
 - area defined by the vectors created with the initial stroke point and consecutive stroke points.
 - good discriminator for straight vs. curved lines

Given $\vec{u}_i = p_{i+1} - p_1$ and $\vec{v}_i = p_{i+2} - p_1$

$$s_{area} = \sum_{i=1}^{n-2} \frac{1}{2} (\vec{u}_i \times \vec{v}_i) \cdot \text{sgn}(\vec{u}_i \times \vec{v}_i)$$

where $\vec{u}_i \times \vec{v}_i$ is a scalar



Geometric Features (5)

- Fit line feature
 - sophisticated approach to finding how close a stroke is to a straight line
 - finds a least-squares approximation to a line using principal components and then uses this approximation to find the distance of the projection of the stroke points onto the approximated line
 - outputs a value in [0,1]
- What is another name for this approach?

Fit Line Feature Implementation

Input: A set of stroke points P .

Output: A distance measure

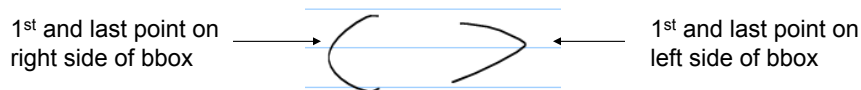
FITLINE(P)

```
(1)  $x_1 \leftarrow \sum_{i=1}^n X(P_i)$ 
(2)  $y_1 \leftarrow \sum_{i=1}^n Y(P_i)$ 
(3)  $x_2 \leftarrow \sum_{i=1}^n X(P_i)^2$ 
(4)  $y_2 \leftarrow \sum_{i=1}^n Y(P_i)^2$ 
(5)  $xy_1 \leftarrow \sum_{i=1}^n X(P_i)Y(P_i)$ 
(6)  $x_3 \leftarrow x_2 - x_1^2/n$ 
(7)  $y_3 \leftarrow y_2 - y_1^2/n$ 
(8)  $xy_2 \leftarrow xy_1 - (x_1y_1)/n$ 
(9)  $rad \leftarrow \sqrt{(x_3 - y_3)^2 + 4xy_2}$ 
(10)  $error \leftarrow (x_3 + y_3 - rad)/2$ 
(11)  $rms \leftarrow \sqrt{error/n}$ 
(12) if  $x_3 > y_3$ 
(13)    $a \leftarrow -2xy_2$ 
(14)    $b \leftarrow x_3 - y_3 + rad$ 
(15) else if  $x_3 < y_3$ 
(16)    $a \leftarrow y_3 - x_3 + rad$ 
(17)    $b \leftarrow -2xy_2$ 
(18) else
(19)   if  $xy_2 = 0$ 
(20)      $a \leftarrow b \leftarrow c \leftarrow 0$ 
(21)      $error \leftarrow +\infty$ 
(22)   else
(23)      $a \leftarrow 1$ 
(24)      $b \leftarrow -1$ 
(25)      $mag \leftarrow \sqrt{a^2 + b^2}$ 
(26)      $c \leftarrow \frac{(-ax_1 - by_1)/n}{mag}$ 
(27)      $a \leftarrow \frac{a}{mag}$ 
(28)      $b \leftarrow \frac{b}{mag}$ 
(29)      $min_1 \leftarrow +\infty$ 
(30)      $max_1 \leftarrow -\infty$ 
(31)     for  $i=1$  to  $n$ 
(32)        $err \leftarrow aX(P_i) + bY(P_i) + c$ 
(33)        $pX \leftarrow X(P_i) - a \cdot err$ 
(34)        $pY \leftarrow Y(P_i) - b \cdot err$ 
(35)        $ploc \leftarrow -b \cdot pX + b \cdot pY$ 
(36)        $min_1 \leftarrow \min(min_1, ploc)$ 
(37)        $max_1 \leftarrow \max(max_1, ploc)$ 
(38)     return  $\frac{100 \cdot rms}{max_1 - min_1}$ 
```

Statistical Features (1)

■ Side ratios

- first and last point of strokes have variable locations with respect to the bounding box
- Approach
 - take the x coordinates of the first and last point of a stroke
 - subtract them from the left side of the symbol's bounding box (i.e., the bounding box's leftmost x value)
 - divide by the bounding box width.



Fall 2012

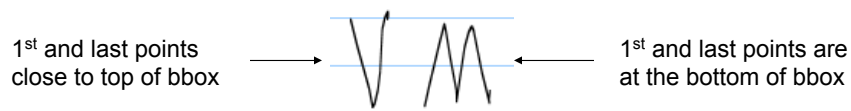
CAP 6105 – Pen-Based User Interfaces

©Joseph J. LaViola Jr.

Statistical Features (2)

■ Top and Bottom ratios

- similar to side ratios except we are dealing with y coordinate
- approach
 - take y coordinate of the first and last point of a stroke
 - subtract from the top of the symbol's bounding box (i.e., the bounding box's topmost y value)
 - these values are divided by the bounding box height.



Fall 2012

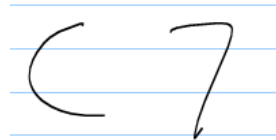
CAP 6105 – Pen-Based User Interfaces

©Joseph J. LaViola Jr.

Statistical Features (3)

■ Point Histogram

- distribution of point locations in stroke bounding box
- discrimination where point concentrations are high
- approach
 - break up box into $n \times m$ grid
 - Count number of points in each sub box
 - divide by total number of points



Statistical Features (4)

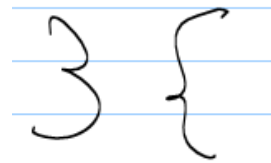
■ Angle Histogram

- similar to point histogram except dealing with angles
- Approach

Given $\vec{v}_j = p_i - p_{i-1}$ for $2 \leq i \leq n$ and $\vec{x} = (1,0)$

$$\alpha_j = \arccos \left(\frac{\vec{x} \cdot \vec{v}_j}{\|\vec{v}_j\|} \right)$$

- put angles into bins of n degrees



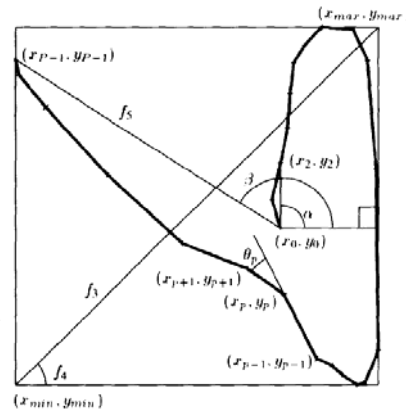
The Rubine Feature Set (Rubine 1991)

- Part of Rubine's gesture recognition system

- we will see this next class

- Stroke

- P = total number of points
- p = middle point
- first point (x_0, y_0, t_0)
- last point $(x_{P-1}, y_{P-1}, t_{P-1})$
- compute x_{min} , y_{min} , x_{max} , y_{max}



Fall 2012

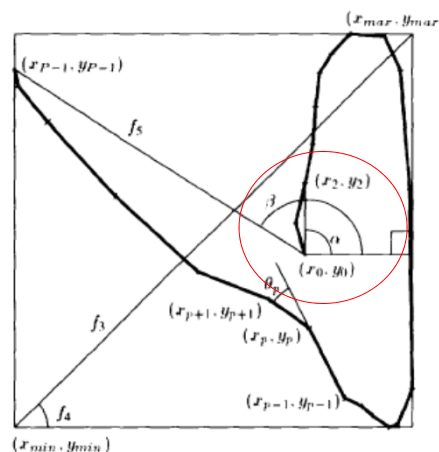
CAP 6105 – Pen-Based User Interfaces

©Joseph J. LaViola Jr.

Feature f_1

- Cosine of starting angle

$$f_1 = \cos(\alpha) = \frac{(x_2 - x_0)}{\sqrt{(x_2 - x_0)^2 + (y_2 - y_0)^2}}$$



Fall 2012

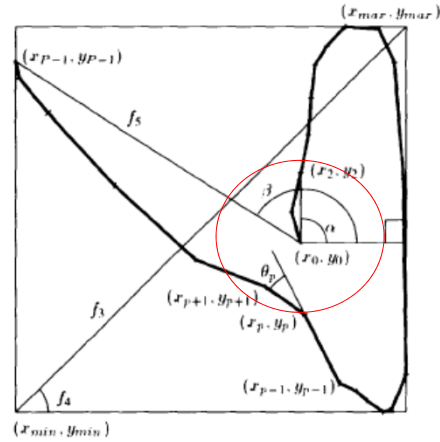
CAP 6105 – Pen-Based User Interfaces

©Joseph J. LaViola Jr.

Feature f_2

- Sine of starting angle

$$f_2 = \sin(\alpha) = \frac{(y_2 - y_0)}{\sqrt{(x_2 - x_0)^2 + (y_2 - y_0)^2}}$$



Fall 2012

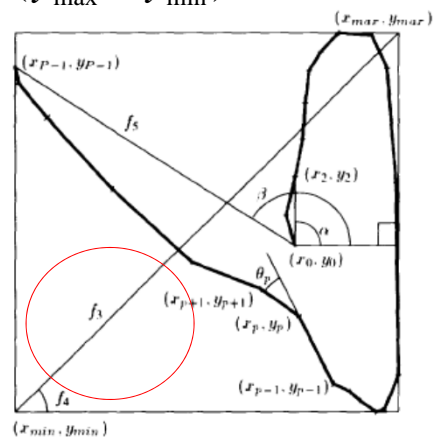
CAP 6105 – Pen-Based User Interfaces

©Joseph J. LaViola Jr.

Feature f_3

$$f_3 = \sqrt{(x_{\max} - x_{\min})^2 + (y_{\max} - y_{\min})^2}$$

- Length of diagonal of bounding box (gives an idea of the size of the bounding box)



Fall 2012

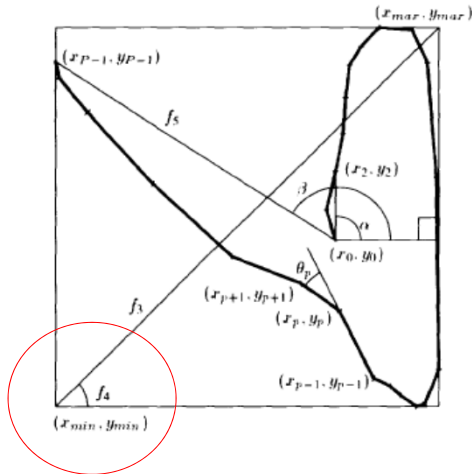
CAP 6105 – Pen-Based User Interfaces

©Joseph J. LaViola Jr.

Feature f_4

- Angle of diagonal
- gives an idea of the shape of the bounding box (long, tall, square)

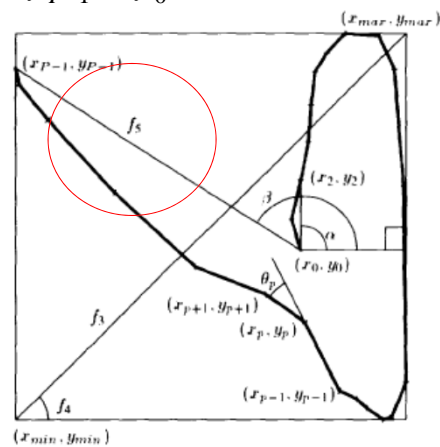
$$f_4 = \arctan\left(\frac{y_{\max} - y_{\min}}{x_{\max} - x_{\min}}\right)$$



Feature f_5

$$f_5 = \sqrt{(x_{p-1} - x_0)^2 + (y_{p-1} - y_0)^2}$$

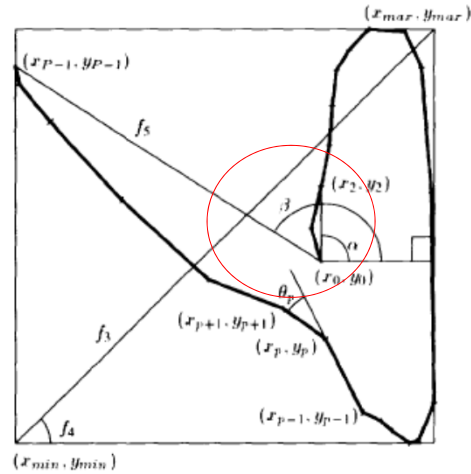
- Distance from start to end of stroke



Feature f_6

- Cosine of ending angle

$$f_6 = \cos(\beta) = \frac{(x_{p-1} - x_0)}{f_5}$$



Fall 2012

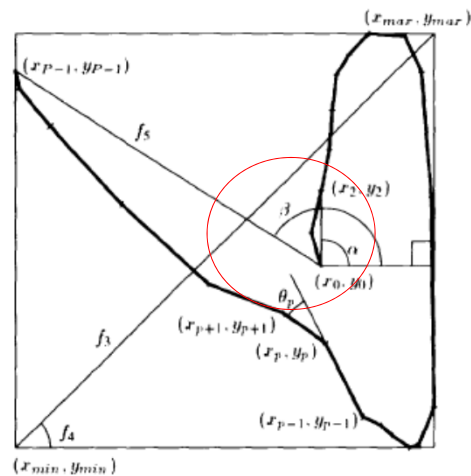
CAP 6105 – Pen-Based User Interfaces

©Joseph J. LaViola Jr.

Feature f_7

- Sine of ending angle

$$f_7 = \sin(\beta) = \frac{(x_{p-1} - x_0)}{f_5}$$



Fall 2012

CAP 6105 – Pen-Based User Interfaces

©Joseph J. LaViola Jr.

More Definitions (before we continue)

Let $\Delta x_p = x_{p+1} - x_p$ and $\Delta y_p = y_{p+1} - y_p$

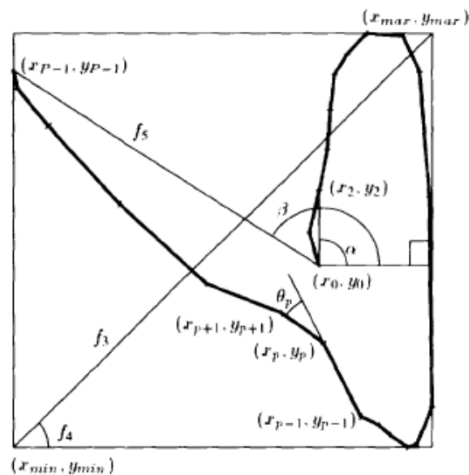
Let $\theta_p = \arctan \frac{\Delta x_p \Delta y_{p-1} - \Delta x_{p-1} \Delta y_p}{\Delta x_p \Delta x_{p-1} + \Delta y_p \Delta y_{p-1}}$ Directional angle

Let $\Delta t_p = t_{p+1} - t_p$ Time delta

Feature f_8

- Total stroke length

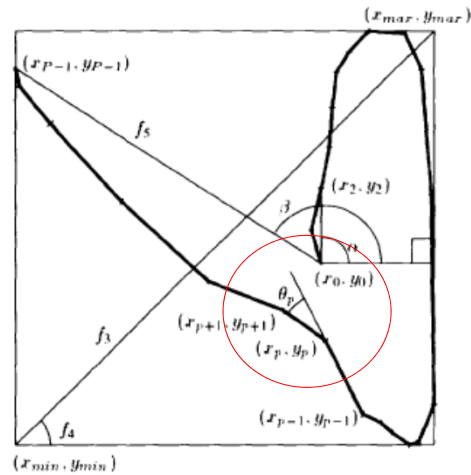
$$f_8 = \sum_{p=0}^{P-2} \sqrt{\Delta x_p^2 + \Delta y_p^2}$$



Feature f_9

- Total rotation (from start to end point)
- (not the same as $\beta - \alpha$ – think of spirals)

$$f_9 = \sum_{p=1}^{P-2} \theta_p$$



Fall 2012

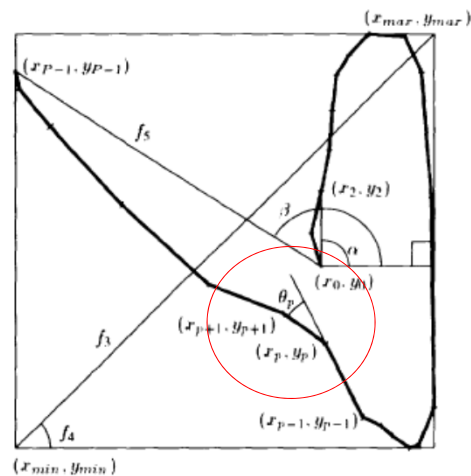
CAP 6105 – Pen-Based User Interfaces

©Joseph J. LaViola Jr.

Feature f_{10}

- Absolute rotation
- How much does it move around

$$f_{10} = \sum_{p=1}^{P-2} |\theta_p|$$



Fall 2012

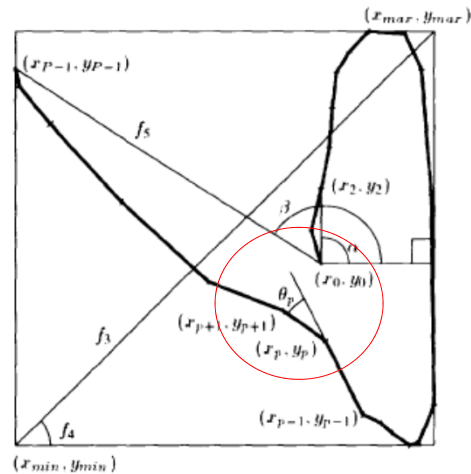
CAP 6105 – Pen-Based User Interfaces

©Joseph J. LaViola Jr.

Feature f_{11}

- Rotation squared
- How smooth are the turns?
- Measure of sharpness

$$f_{11} = \sum_{p=1}^{P-2} \theta_p^2$$



Fall 2012

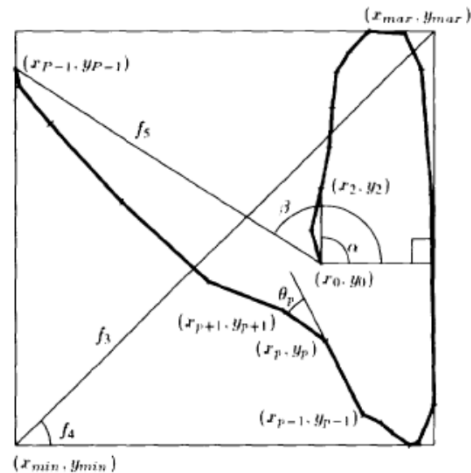
CAP 6105 – Pen-Based User Interfaces

©Joseph J. LaViola Jr.

Feature f_{12}

- The maximum speed reached (squared)

$$f_{12} = \max_{p=0}^{P-2} \frac{\Delta x_p^2 + \Delta y_p^2}{\Delta t_p^2}$$



Fall 2012

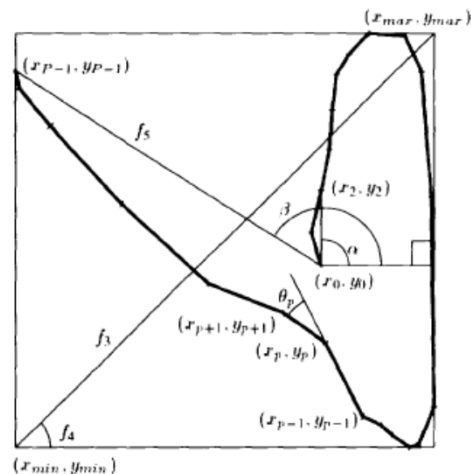
CAP 6105 – Pen-Based User Interfaces

©Joseph J. LaViola Jr.

Feature f_{13}

- Total time of stroke

$$f_{13} = t_{P-1} - t_0$$



Readings

- LaViola, J., and Zeleznik, R. "A Practical Approach to Writer-Dependent Symbol Recognition Using a Writer-Independent Recognizer", IEEE Transactions on Pattern Analysis and Machine Intelligence, 29(11):1917-1926, November 2007.
- Herold, J., and Staohvich, T. ClassySeg: A Machine Learning Approach to Automatic Stroke Segmentation. In *Proceedings of the Eighth Eurographics/ACM Symposium on Sketch-Based Interfaces and Modeling 2011*, 109-116, August 2011.
- Blagojevic, R., Chang, S., and Plimmer, B. The Power of Automatic Feature Selection: Rubine on Steroids, In *Proceedings of the Seventh Eurographics/ACM Symposium on Sketch-Based Interfaces and Modeling 2010*, 79-86, June 2010.
- Wobbrock, J. O., Wilson, A. D., and Li, Y. 2007. Gestures without libraries, toolkits or training: a \$1 recognizer for user interface prototypes. In *Proceedings of the 20th Annual ACM Symposium on User Interface Software and Technology UIST '07*. ACM, New York, NY, 159-168.