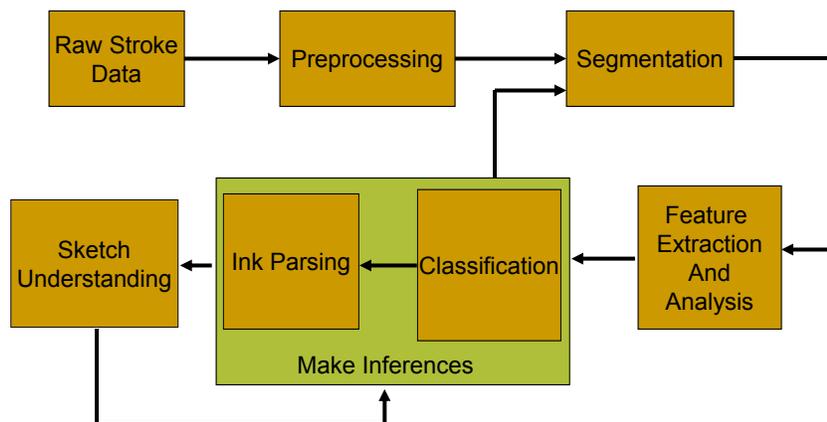


# Ink Segmentation

Lecture #7: Ink Segmentation  
Joseph J. LaViola Jr.  
Fall 2011

# Recall Pen-Based Interface Dataflow



## Segmentation

- Determine which strokes go together
- Determine which strokes should be apart
- Can be done in real-time or in batch
- Often uses proximity and timing information

$$y = \frac{1}{2} x^2$$
$$y = x^2 e^{-\frac{1}{2}t}$$

5 K 

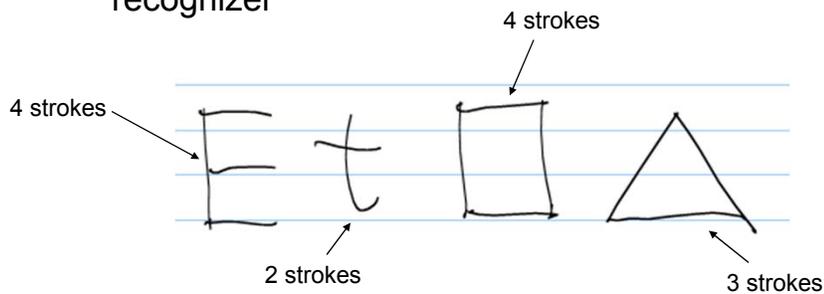
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## Grouping Strokes Together

- Why? – Multiple strokes can form one symbol
  - math symbols, shapes, etc...
  - want to pass all strokes that make up a symbol to recognizer



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## Grouping Strokes Together – Basic Approach

- Check to see if two or more strokes intersect
  - if they do then group them together
- Can use simple line segment intersection tests
- Problems
  - ink strokes – ink  $\neq$  polyline
  - what if two strokes do not intersect but should be grouped together?
  - what if two strokes intersect but should not be grouped together?

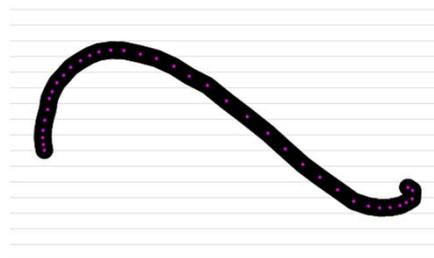
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## Ink Strokes and Polylines

- Polylines are internal representation
- Ink has width
  - need requires more robust intersection
- One approach
  - find silhouettes
  - do intersection testing on them



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## Robust Stroke Intersection (Part 1)

**Input:** Stroke  $s_i$ , a set of candidate strokes  $CS = \{s_1, s_2, \dots, s_n\}$ .

**Output:** True or false

ROBUSTINTERSECTION( $s_i, CS$ )

- (1)  $P \leftarrow Points(s_i)$
- (2)  $cs_1 \leftarrow Circle(P_1, \frac{PenInkWidth()}{2})$
- (3)  $cs_2 \leftarrow Circle(P_n, \frac{PenInkWidth()}{2})$
- (4)  $sil_1 \leftarrow Polygon(ComputeStrokeEdges(s_i))$
- (5) **foreach** Stroke  $stk \in CS$
- (6)      $Q \leftarrow Points(stk)$
- (7)      $cstk_1 \leftarrow Circle(Q_1, \frac{PenInkWidth()}{2})$
- (8)      $cstk_2 \leftarrow Circle(Q_n, \frac{PenInkWidth()}{2})$
- (9)      $sil_2 \leftarrow Polygon(ComputeStrokeEdges(stk))$
- (10)    **if**  $cs_1 \cap cstk_1$  **or**  $cs_1 \cap cstk_2$  **or**  $cs_1 \cap sil_2$  **or**  $cs_2 \cap cstk_1$  **or**  $cs_2 \cap cstk_2$   
      **or**  $cs_2 \cap sil_2$  **or**  $sil_1 \cap cstk_1$  **or**  $sil_1 \cap cstk_2$  **or**  $sil_1 \cap sil_2$
- (11)    **return true**
- (12) **return false**

## Robust Stroke Intersection (Part 2)

**Input:** Stroke  $s_i$

**Output:** A list of silhouette points

COMPUTESTROKEEDGES( $s_i$ .)

- (1)  $P \leftarrow Points(s_i)$
- (2)  $pen_w \leftarrow \frac{PenInkWidth()}{2}$
- (3) **if**  $n < 3$
- (4)     **return**  $P$
- (5) **for**  $i = 1$  **to**  $n - 1$
- (6)      $\vec{v}_1 \leftarrow Vector(Y(P_{i+1}) - Y(P_i), -(X(P_{i+1}) - X(P_i)))$
- (7)      $\vec{v}_2 \leftarrow Vector(-(Y(P_{i+1}) - Y(P_i)), X(P_{i+1}) - X(P_i))$
- (8)      $Ppts1_i \leftarrow P_i + pen_w \frac{\vec{v}_1}{\|\vec{v}_1\|}$
- (9)      $Ppts2_i \leftarrow P_i + pen_w \frac{\vec{v}_2}{\|\vec{v}_2\|}$
- (10)    **if**  $i = n - 1$
- (11)      $Ppts1_i \leftarrow P_{i+1} + pen_w \frac{\vec{v}_1}{\|\vec{v}_1\|}$
- (12)      $Ppts2_i \leftarrow P_{i+1} + pen_w \frac{\vec{v}_2}{\|\vec{v}_2\|}$

## Robust Intersection (Part 2) –cont'd

```

(13) for  $i = 1$  to  $n - 1$ 
(14)   if  $i = 1$ 
(15)      $Silpts1_i = Ppts1_i$ 
(16)      $Silpts2_i = Ppts2_i$ 
(17)     continue
(18)   if  $i = n - 1$ 
(19)      $Silpts1_{i+1} = Ppts1_{i+1}$ 
(20)      $Silpts2_{i+1} = Ppts2_{i+1}$ 
(21)     continue
(22)    $\vec{v}_3 \leftarrow \text{Vector}(X(Ppts1_{i-1}) - X(Ppts1_i), Y(Ppts1_{i-1}) - Y(Ppts1_i))$ 
(23)    $\vec{v}_4 \leftarrow \text{Vector}(X(Ppts1_i) - X(Ppts1_{i+1}), Y(Ppts1_i) - Y(Ppts1_{i+1}))$ 
(24)    $intpt \leftarrow \text{LineIntersection}(Ppts1_i, \frac{\vec{v}_3}{\|\vec{v}_3\|}, Ppts1_{i+1}, \frac{\vec{v}_4}{\|\vec{v}_4\|})$ 
(25)   if  $intpt = \emptyset$ 
(26)      $Silpts1_i = Ppts1_i$ 
(27)   else
(28)      $Silpts1_i = intpt$ 
(29)    $\vec{v}_5 \leftarrow \text{Vector}(X(Ppts2_{i-1}) - X(Ppts2_i), Y(Ppts2_{i-1}) - Y(Ppts2_i))$ 
(30)    $\vec{v}_6 \leftarrow \text{Vector}(X(Ppts2_i) - X(Ppts2_{i+1}), Y(Ppts2_i) - Y(Ppts2_{i+1}))$ 
(31)    $intpt \leftarrow \text{LineIntersection}(Ppts2_i, \frac{\vec{v}_5}{\|\vec{v}_5\|}, Ppts2_{i+1}, \frac{\vec{v}_6}{\|\vec{v}_6\|})$ 
(32)   if  $intpt = \emptyset$ 
(33)      $Silpts2_i = Ppts2_i$ 
(34)   else
(35)      $Silpts2_i = intpt$ 
(36) return  $\text{CreatePointList}(Silpts1, Silpts2, Silpts1_0)$ 

```

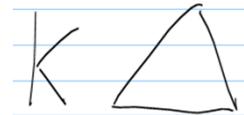
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## Grouping Strokes Together – Extending Basic Approach

- What if two or more strokes should be grouped together but do not intersect?
- Need other information
  - timing info
  - spatial info
- If two strokes are close together and they have been drawn consecutively then there is a good chance they should be grouped together
  - still has problems



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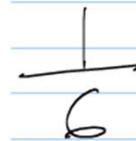
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## Grouping Strokes Together – Using Recognition

- To help with segmentation – use recognizer (Smithies et. al 1999)
- For each stroke
  - take last k strokes and send to recognizer
  - look for symbol recognitions with highest confidence level
  - group based on highest confidence level
- When all else fails
  - use domain knowledge
  - easy to use UI correction techniques

## Inadvertent Stroke Grouping

- What if strokes are intersecting but should not be grouped together?
- Must look at context
  - would such a symbol make sense in its surroundings?
  - example – perpendicular symbol over 6 does not make sense (so ungroup to make 1 and division line)
- UI correction also important (tools for breaking strokes apart)

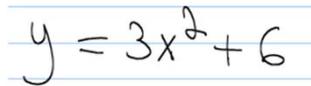


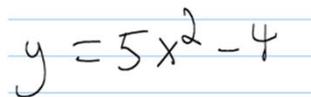
## Breaking Strokes Apart

- Why? – Want to break symbols (groups of strokes) into logical blocks
  - Examples include mathematical expressions on a page, multiple diagrams or drawings
- Starts moving into sketch understanding and sketch parsing
- As with grouping, using recognition engine can help
- Domain knowledge also important

## Breaking Strokes Apart – Basic Approach

- Lines of math
- Do a horizontal line sweep, if white space is found, break up strokes into expressions
  - a threshold could be used just in case of a few pixels found in sweep
- Another approach
  - Look at histogram of points
    - rotate ink 90 degrees
    - project onto x-axis
    - find minima


$$y = 3x^2 + 6$$


$$y = 5x^2 - 4$$

## Strategy Summary

- Can go a long way with speed data, proximity info, and intersection testing
  - does not work every time
- Use recognizer to help find segmentations that make sense
- Make use of domain knowledge
- Have easy to use UI techniques for corrections
- More on this when we get to sketch understanding

## Readings

- Gennari, L., L. Kara, and T. Stahovich. Combining geometry and domain knowledge to interpret hand drawn diagrams, *Computers and Graphics*, 29(4):547-562, 2005.
- Peterson, E., Stahovich, T., Doi, E., and Alvarado, C. Grouping Strokes into Shapes in Hand-Drawn Diagrams *Proc. of the 24th AAAI Conference on Artificial Intelligence (AAAI-10)*, 2010, pp. 974-979
- Tevfik Metin Sezgin and Randall Davis. Sketch Interpretation Using Multiscale Models of Temporal Patterns. In *IEEE Journal of Computer Graphics and Applications*, Volume: 27, Issue: 1, pp: 28-37, 2007.