

(3). How many times have each process use the NIC service?

(4). For each process, what is the average waiting time respectively when it waits in the NIC queue?

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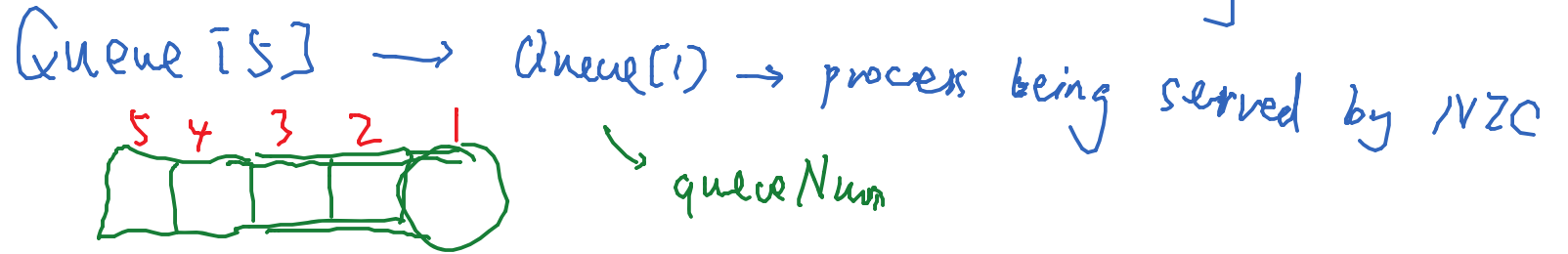
- Process 5 has the largest number of NIC visit.
- Process 1 & 2 have similar # \rightarrow smallest #
- Process 5 waiting time < 5 sec

Event List [5]
 Status: ["Using other resource", "waiting" in queue, "Using NIC"]

$$-\ln U/A$$

s-th erlang : $= -\frac{\ln U_1}{\mu} - \frac{\ln U_2}{\mu} - \frac{\ln U_3}{A} - \frac{\ln U_4}{\mu} - \frac{\ln U_5}{\mu}$
 $= -\ln(\mu_1 \cdot \mu_2 \cdot \mu_3 \cdot \mu_4 \cdot \mu_5) / \mu$

process status = "O" → "N" when NIC is idle
→ "W" when NIC is busy



NIC
Process status "N" → "O"

passive event: "W" → "N"

$$\pi_0 \lambda = \pi_1 \mu \Rightarrow \pi_1 = \rho \pi_0$$

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$$\pi_1 \lambda = \pi_2 \mu \Rightarrow \pi_2 = \rho^2 \pi_0$$

\vdots

$$\pi_{n-1} \lambda = \pi_n \mu \Rightarrow \pi_n = \rho^n \pi_0$$

$$\begin{aligned} \pi_2 &= \frac{\lambda}{\mu} \pi_1 = \rho \pi_1 = \rho^2 \pi_0 \\ \pi_n &= \rho^n \pi_0 \end{aligned}$$

$$\sum_{i=0}^{\infty} \pi_i = 1 \Rightarrow \pi_0 + \rho \pi_0 + \rho^2 \pi_0 + \rho^3 \pi_0 + \dots = 1$$

$$\Rightarrow \bar{\lambda}_0 = \frac{1}{S} = 1 - \rho$$

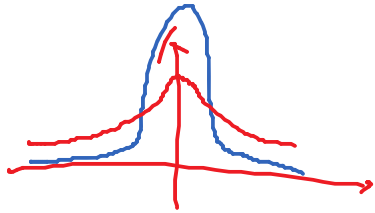
$$S = 1 + \rho + \rho^2 + \rho^3 + \dots$$

$$\rightarrow \rho S = \rho + \rho^2 + \rho^3 + \rho^4 + \dots$$

$$(1-\rho)S = 1 + \rho^n \underset{n \rightarrow \infty}{=} 1 \Rightarrow S = \frac{1}{1-\rho}$$

Exp. distr. $\lambda = 0.2/\text{sec} \rightarrow \text{mean} = \frac{1}{\lambda} = 5 \text{ sec}$

5-th Erlang distr. $\mu = 1/\text{sec} \rightarrow \text{mean} = \frac{5}{\mu} = 5 \text{ sec}$



$$E[N] = \sum_{k=1}^{\infty} k \pi_k = \pi_0 \sum_{k=1}^{\infty} k \rho^k = \frac{\rho}{1-\rho}$$

$$\pi_0 = 1-\rho$$

$$E[W] = E[N] \cdot E[X] \quad \leftarrow \frac{1}{\mu}$$

$$= \frac{\rho/\mu}{1-\rho} \cdot \frac{1}{\mu} = \frac{\rho}{\mu(1-\rho)}$$

$$S = \rho + 2\rho^2 + 3\rho^3 + 4\rho^4 + \dots$$

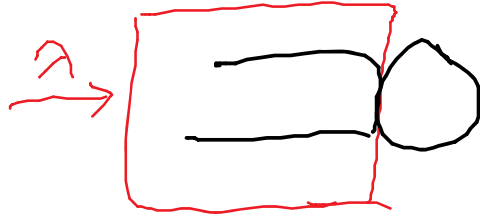
$$\rightarrow \rho S = \rho^2 + 2\rho^3 + 3\rho^4 + 4\rho^5 + \dots$$

$$(1-\rho)S = \rho + \rho^2 + \rho^3 + \rho^4 + \dots = \frac{\rho}{1-\rho}$$

$$\Rightarrow S = \frac{\rho}{(1-\rho)^2} \Rightarrow E[N] = \frac{\rho}{1-\rho}$$

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$$E[T] = \frac{1}{\mu} + E[W] = \frac{1}{\mu} + \frac{\lambda}{\mu(\mu-\lambda)} = \frac{\mu-\lambda + \lambda}{\mu(\mu-\lambda)} = \frac{1}{\mu-\lambda} = \frac{1}{1-\rho} \cdot \frac{1}{\mu}$$



$N = \lambda T$
 N : # of jobs in waiting queue
 T : time in waiting