

$$P_i = p \cdot P_{i+1} + q \cdot P_{i-1}$$

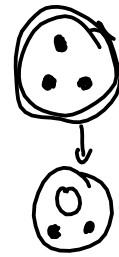
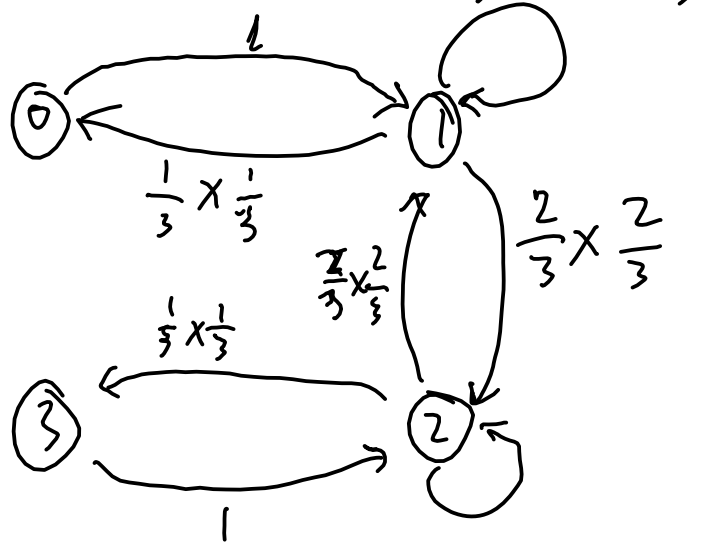
$$P_0 = 0 \quad P_N = 1$$

$$\begin{cases} P_1 = p P_2 \\ P_2 = p P_3 + q P_1 \\ \vdots \\ P_{N-1} = p P_N + q P_{N-2} = p + q P_{N-2} \end{cases}$$

→ $N-1$ linear equations for $N-1$ variables

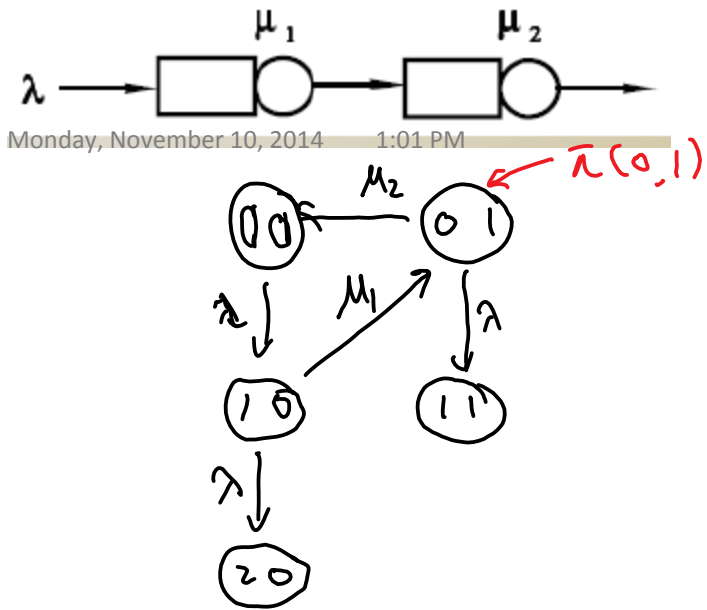
$$X_n = \{0, 1, 2, 3\}$$

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$$P = \begin{bmatrix} 0 & 1 & 2 & 3 \\ 0 & 1 & 0 & 0 \\ 1/9 & 4/9 & 4/9 & 0 \\ 2 & & 4/9 & \\ 3 & & & 0 \end{bmatrix}$$

$$\begin{cases} \pi P = \pi \\ \pi \mathbf{1} = 1 \end{cases}$$

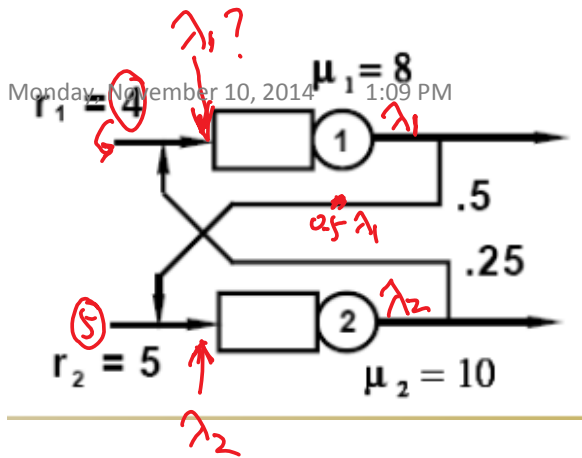


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$$P(N_1 = n_1, N_2 = n_2, \dots, N_k = n_k) = \prod_{i=1}^k (1 - \rho_i) \rho_i^{n_i},$$

$$\rho_i = \frac{\lambda}{\mu_i}$$

$$\pi(i, j) = (1 - \rho_1) \rho_1^i (1 - \rho_2) \rho_2^j \quad i, j \geq 0$$



$$\begin{cases} \lambda_1 = 4 + 0.25 \cdot \lambda_2 \\ \lambda_2 = 5 + 0.5 \cdot \lambda_1 \end{cases}$$

$$\Rightarrow \underline{\lambda_1 = 6, \lambda_2 = 8}$$

$$\rho_1 = \frac{\lambda_1}{\mu_1} = \frac{3}{4}$$

$$\rho_2 = \frac{\lambda_2}{\mu_2} = \frac{4}{5}$$

$$\pi(n_1, n_2) = \frac{1}{4} \left(\frac{3}{4}\right)^{n_1} \frac{1}{5} \left(\frac{4}{5}\right)^{n_2}$$